

## MATERIALE DI SUPPORTO ELICHE E ROTORI AERONAUTICI

### Power

$$P = \frac{1}{2} \dot{m}(V_4^2 - V^2) = \frac{1}{2} \dot{m}(V_4 + V)(V_4 - V) = TV_2 = T(V + v)$$

$$\eta_p = \frac{TV}{TV_2} = \frac{V}{V_2} = \frac{V}{V + v}$$

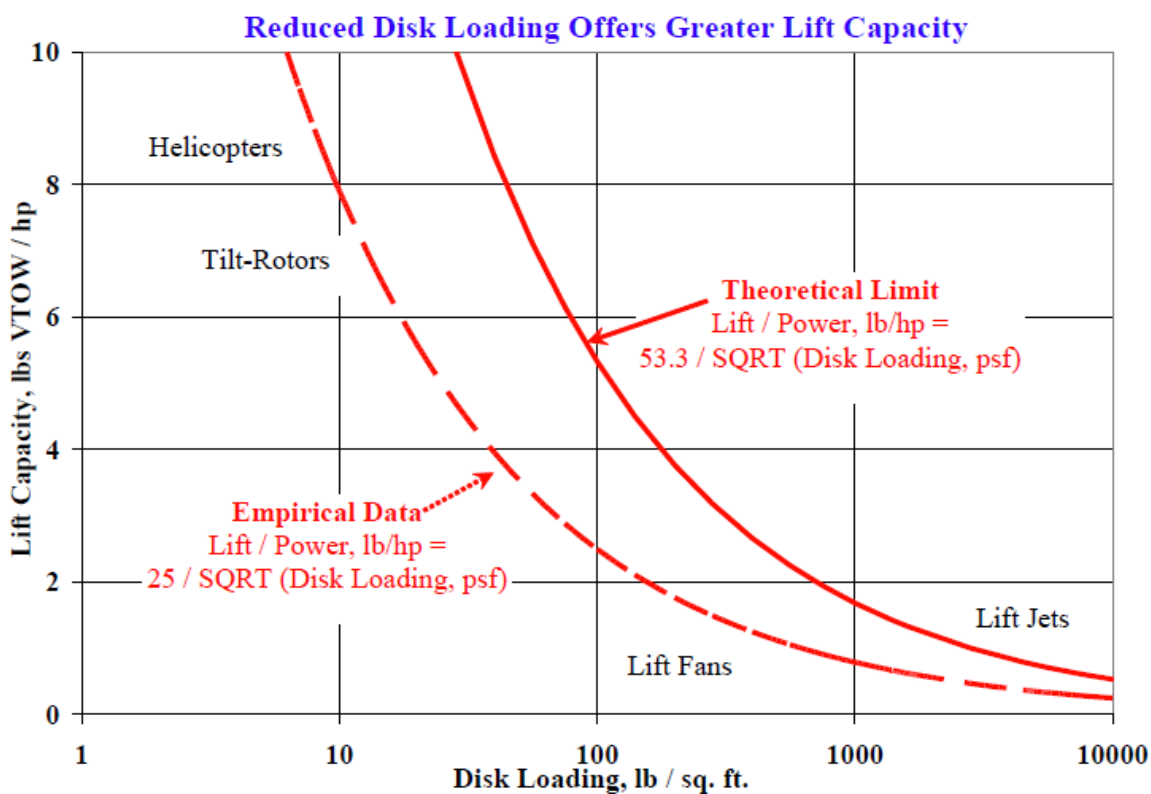
For V=0

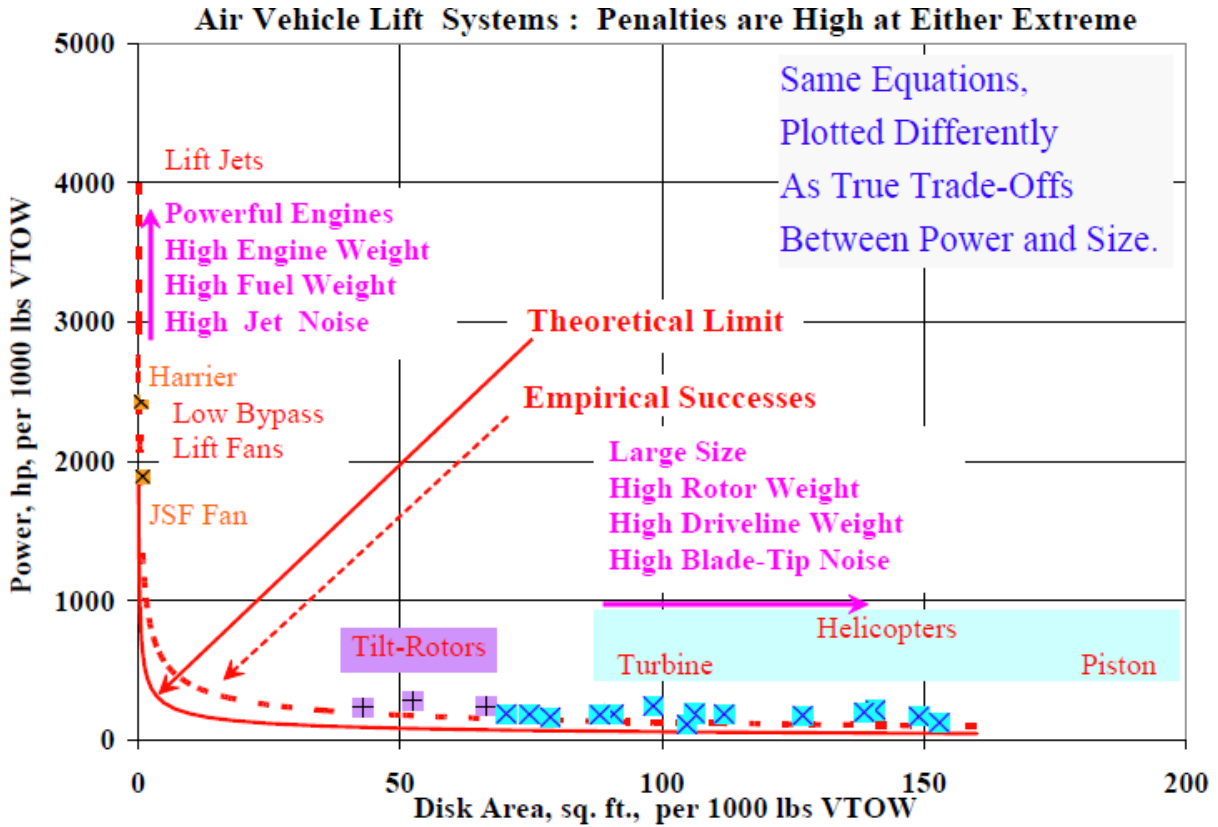
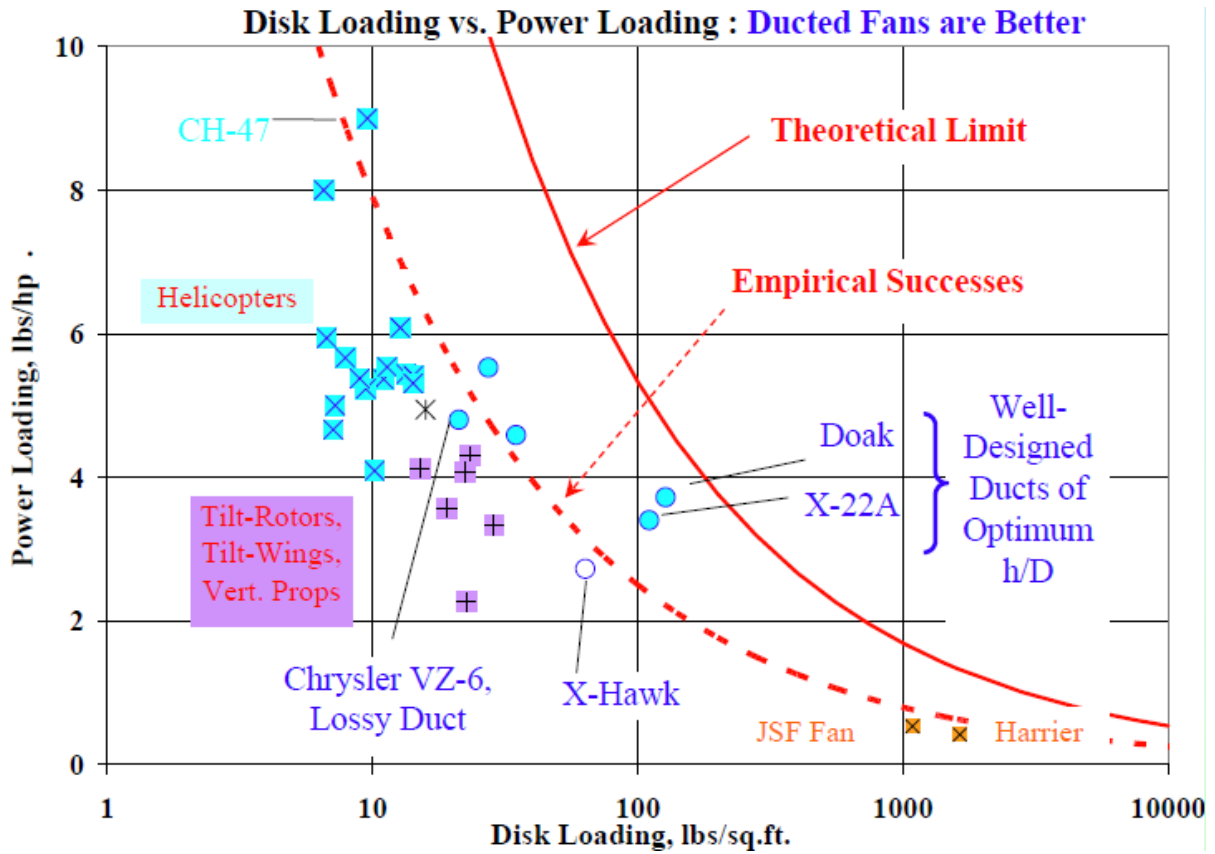
$$v = \left( \frac{T}{2\rho A} \right)^{1/2}$$

$$\frac{P}{A} = \frac{T}{A} V_2 = \frac{T}{A} v \propto \left( \frac{T}{A} \right)^{3/2}$$

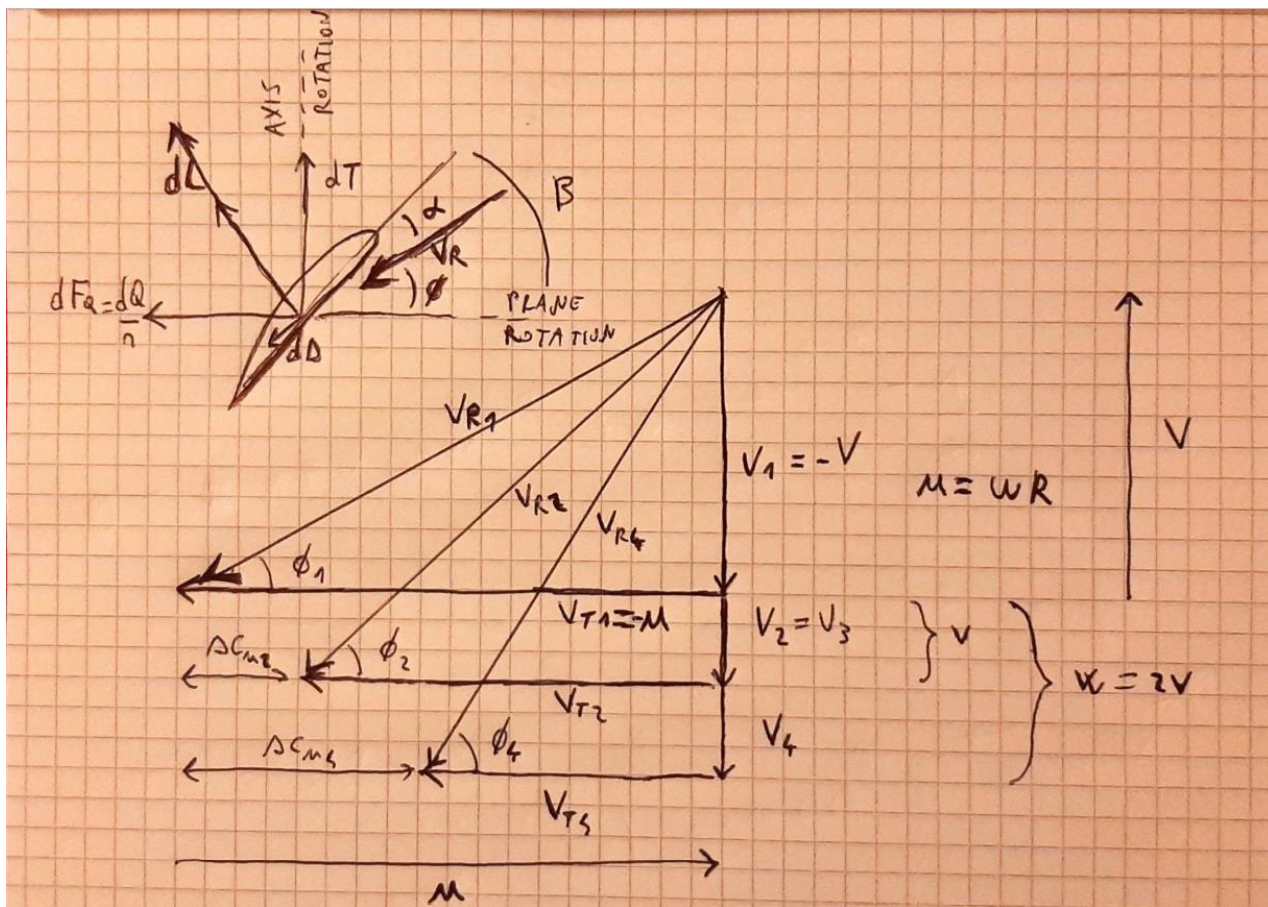
$$\frac{P}{T} \propto \left( \frac{T}{A} \right)^{1/2}$$

$$C_p \propto C_T^{3/2}$$





Triangoli di velocità



Perdite per moti elicoidali

$J' = \frac{V}{u} \propto J = \frac{V}{\pi D}$   
 $C_{DP} = \frac{\Delta P}{\rho u^2} \propto \frac{T/D^2}{\rho \pi^2 D^4} \propto C_T = \frac{T}{\rho \pi^2 D^4}$

$\eta_{conv} = \frac{P_T}{P_{rel}} = \frac{\frac{1}{2} \dot{m} (V_2^2 - V_1^2)}{\dot{m} u \Delta C_M} = \frac{\frac{\Delta P}{\rho}}{u \Delta C_M}$

$\Delta C_M =$  variazione velocità tangenziale flusso d'aria  
 $u R =$  velocità tangenziale elica  
 $Q = \dot{m} R \Delta C_M$  momento variazione momento della q. d. m.  
 $P_{rel} = u Q = \dot{m} u \Delta C_M$

$\eta_{conv} = \frac{u \Delta C_M - \frac{\Delta C_M^2}{2}}{u \Delta C_M} \rightarrow$  energia dissipata per moto elicoidale

$\frac{1}{2} \left( \frac{\Delta C_M}{u} \right)^2 - \frac{\Delta C_M}{u} + \frac{\Delta P}{\rho u^2} = 0 \iff \frac{\Delta P}{\rho} = u \Delta C_M - \frac{\Delta C_M^2}{2}$

$\eta_{conv} = \frac{1 + \sqrt{1 - 2 C_{DP}}}{2} \quad \eta_p = \frac{2}{1 + \sqrt{1 + 2 \frac{C_{DP}}{J^2}}}$

$\eta_{conv} = 1 - \frac{\Delta C_M}{2u} \quad \eta_{el, id} = \eta_p \eta_{conv} = \frac{1 + \sqrt{1 - 2 C_{DP}}}{1 + \sqrt{1 + 2 \frac{C_{DP}}{J^2}}}$



Elica intubata vs Elica libera

$$P = \frac{1}{2} \dot{m} (V_3^2 - V_1^2) \quad T = \Delta p A = \dot{m} (V_3 - V_1)$$

FOR  $V=0$   $P = \frac{1}{2} \dot{m} V_3^2$

$$T = \dot{m} V_4 \quad \dot{m} = \rho A V_2$$

**ELICA INTUBATA  $V_4 = V_2$**

**ELICA LIBERA  $V_3 = 2V_2$**

$$T = \dot{m} V_2 \rightarrow V_2 = \sqrt{\frac{T}{\rho A}}$$

$$T = \dot{m} 2V_2 \rightarrow V_2 = \sqrt{\frac{T}{2\rho A}}$$

51% LARGER

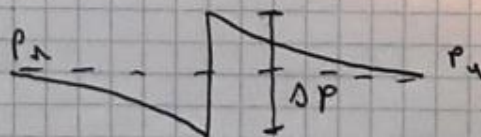
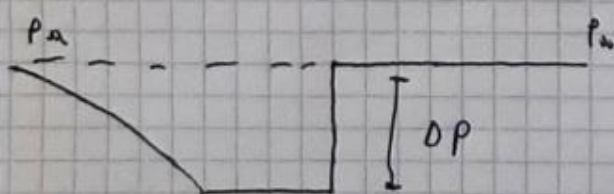
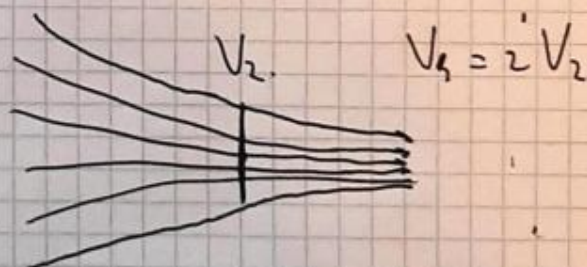
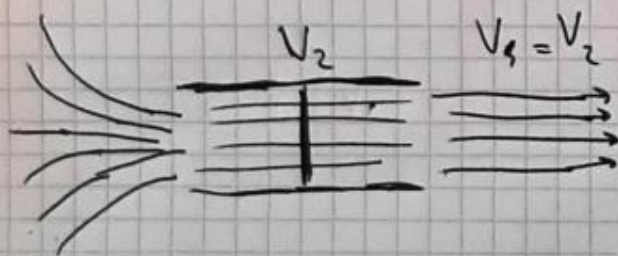
$$P = \frac{1}{2} \dot{m} V_2^2$$

$$= \frac{1}{2} \frac{T^{3/2}}{\sqrt{\rho A}}$$

$$P = \frac{1}{2} \dot{m} (2V_2)^2$$

$$P = \frac{1}{\sqrt{2}} \frac{T^{3/2}}{\sqrt{\rho A}}$$

29% SMALLER!





Zubr class hovercraft (Project 1232.2, NATO reporting name "Pomornik")

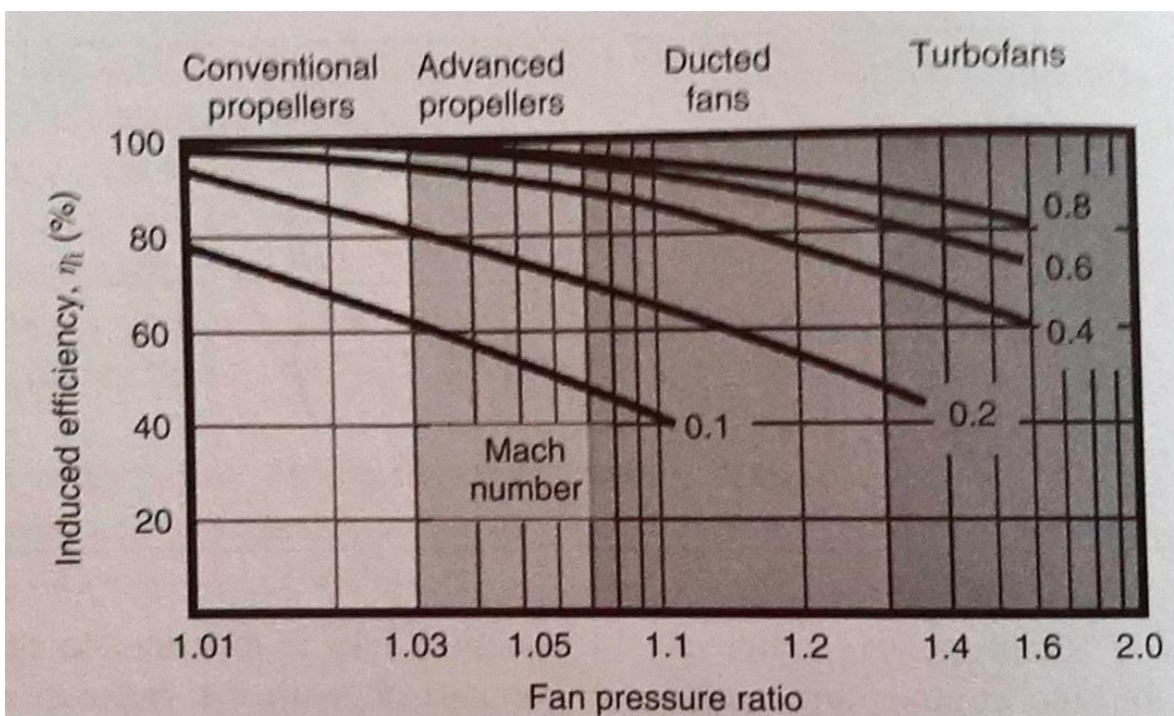
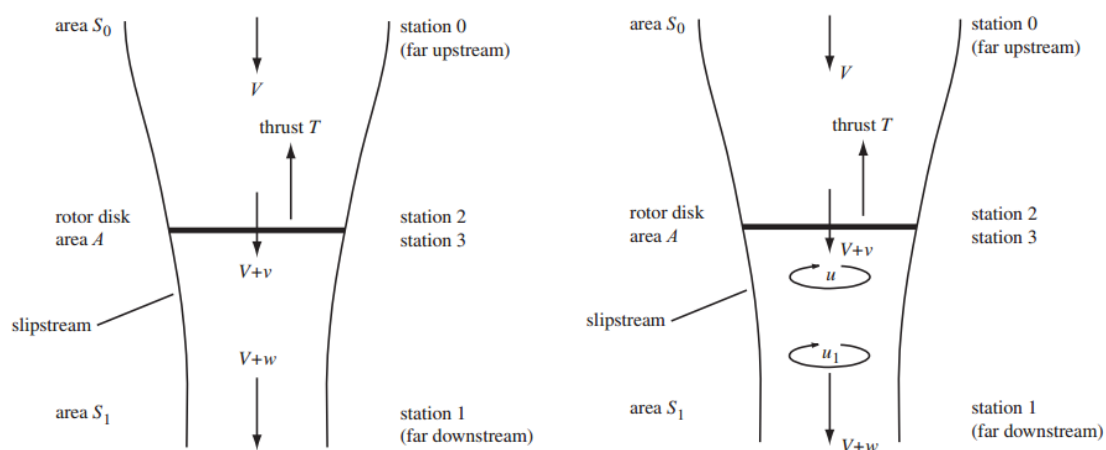


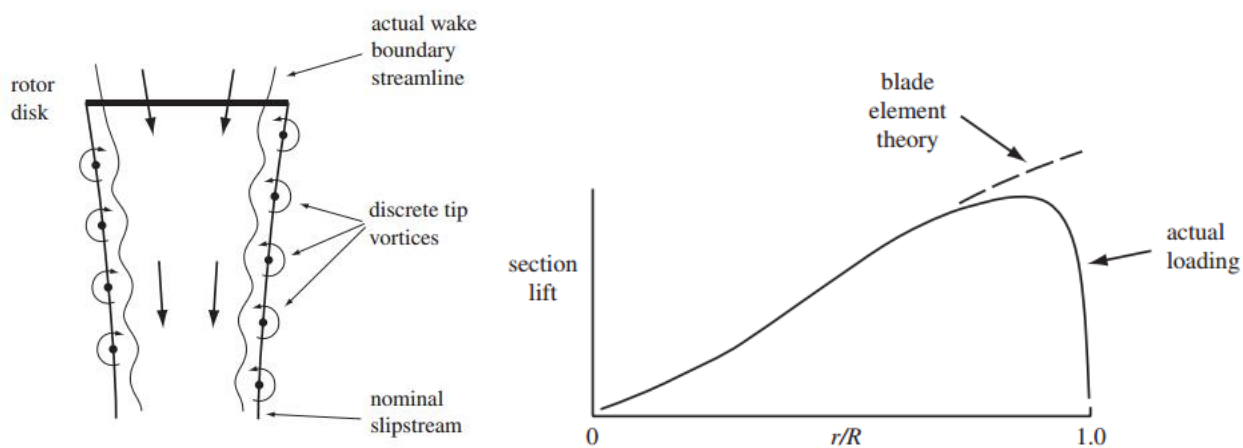
Figure 3.33 Induced efficiency measurements (Courtesy NASA [6].)

Power component	At peak efficiency	Off peak
Ideal induced power	74% to 78%	65%
Profile power	10% to 19%	25%
Nonuniform inflow	5% to 7%	6%
Swirl in the wake	less than 1%	less than 1%
Tip losses	2% to 4%	3%

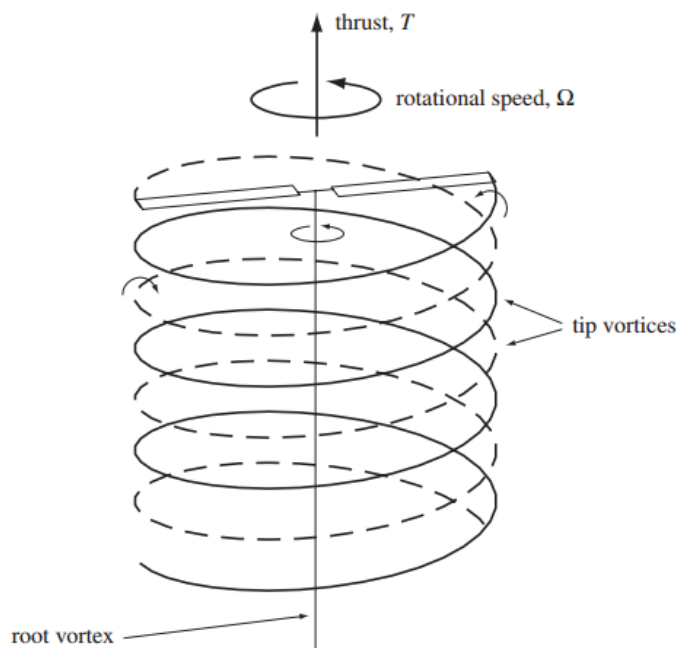
Rotor power components



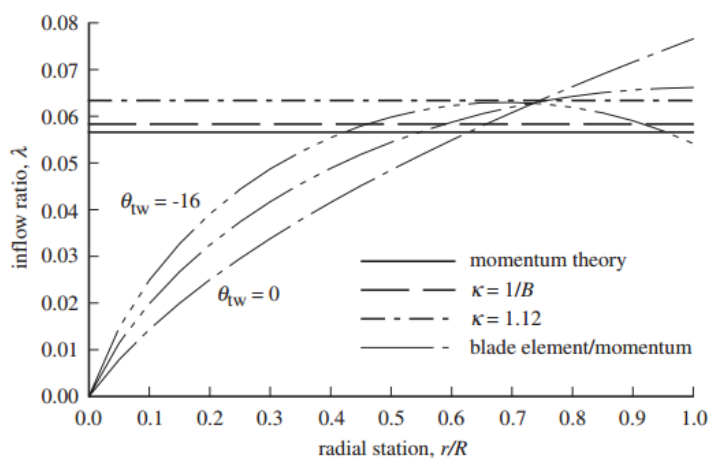
Ideal induced power (left), swirl in the wake (right)



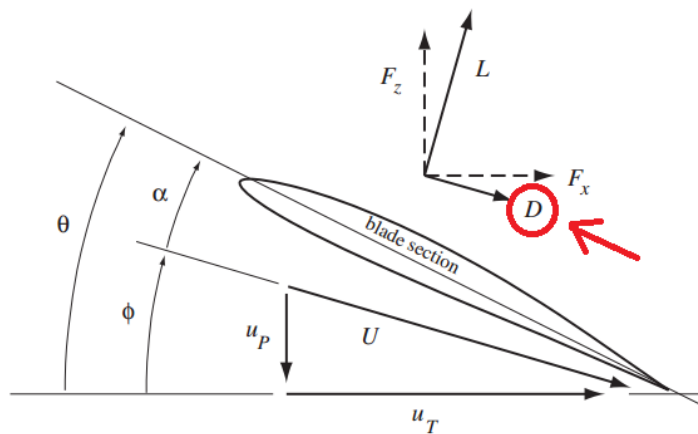
Tip losses



Rotor wake



Non-uniform inflow



Profile losses

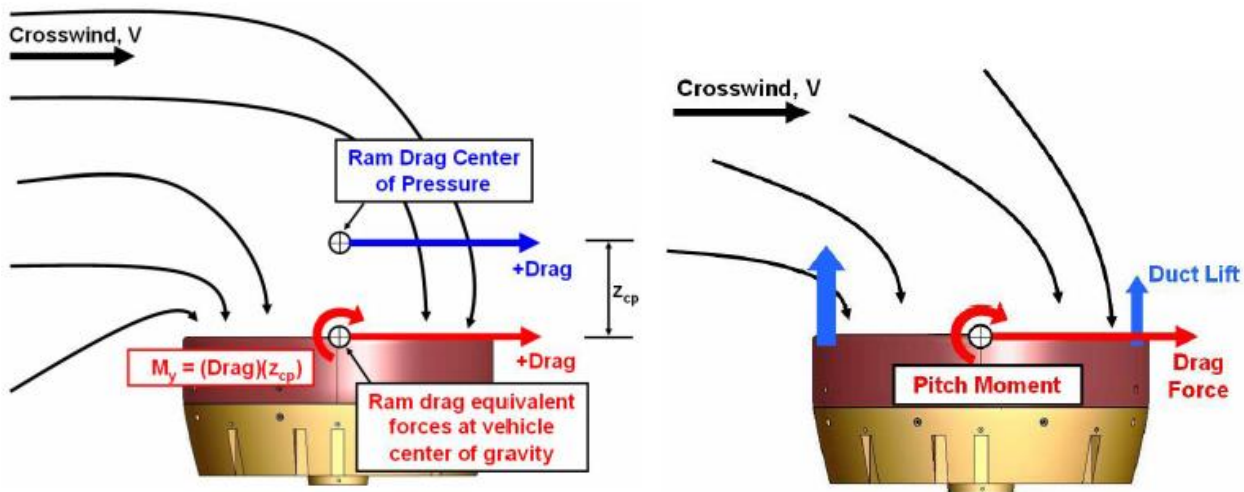




Kamov Ka-50 Black Shark



Boeing CH-47 Chinook



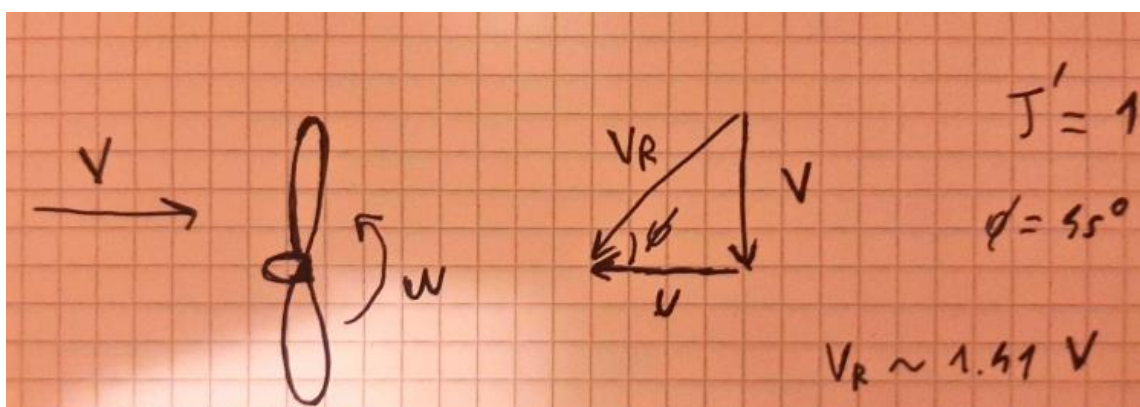
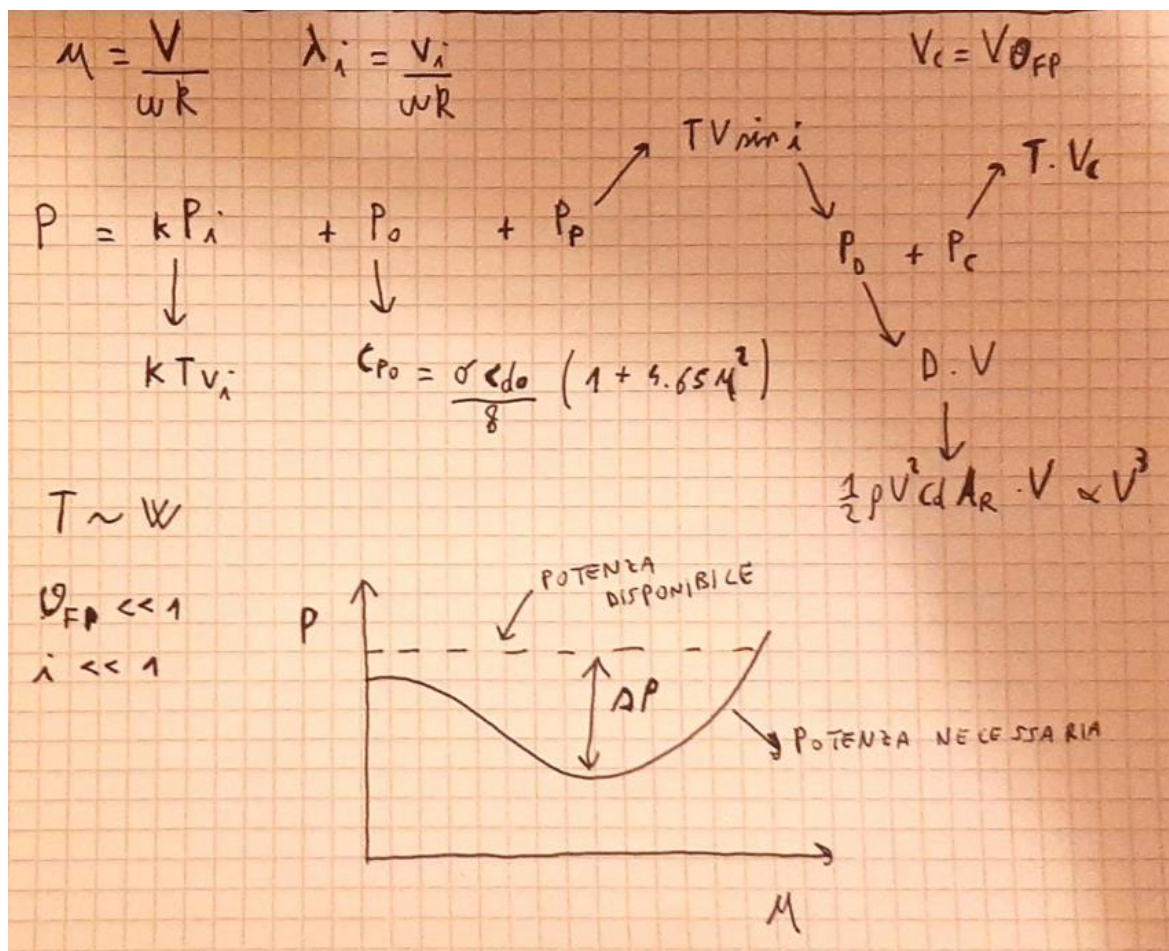
Ram Drag and Pitching Moment of a Ducted Fan in tangential forward flight



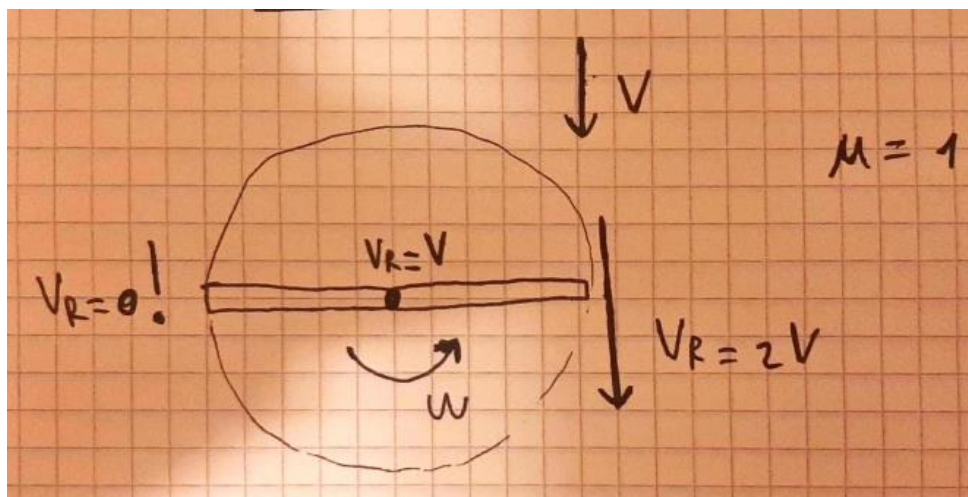
Bell X-22



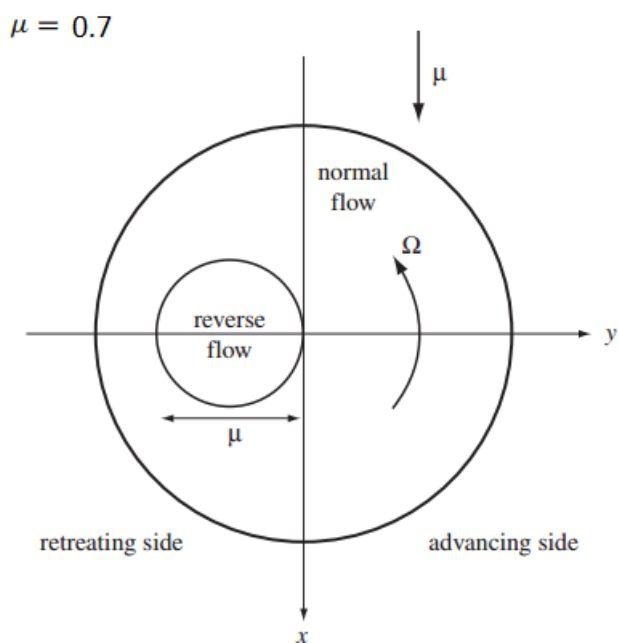
Potenza elicottero



Propeller



Helicopter rotor



Reverse flow region in a helicopter rotor

**How does a Helicopter fly?**

<https://www.youtube.com/watch?v=2tdnqZgKa0E>

**Swashplate (piatto oscillante) animation**

<https://www.youtube.com/watch?v=-kWhNi-MZAM>