



Electric Drives  
Laboratory  
DII - UniPD

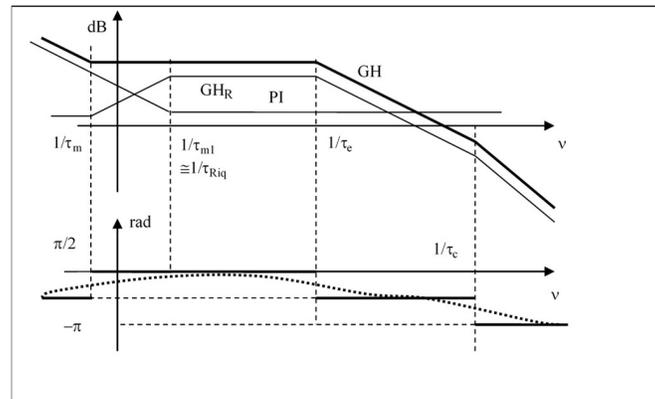
# Azionamenti Elettrici

Lezioni a.a. 2018-2019

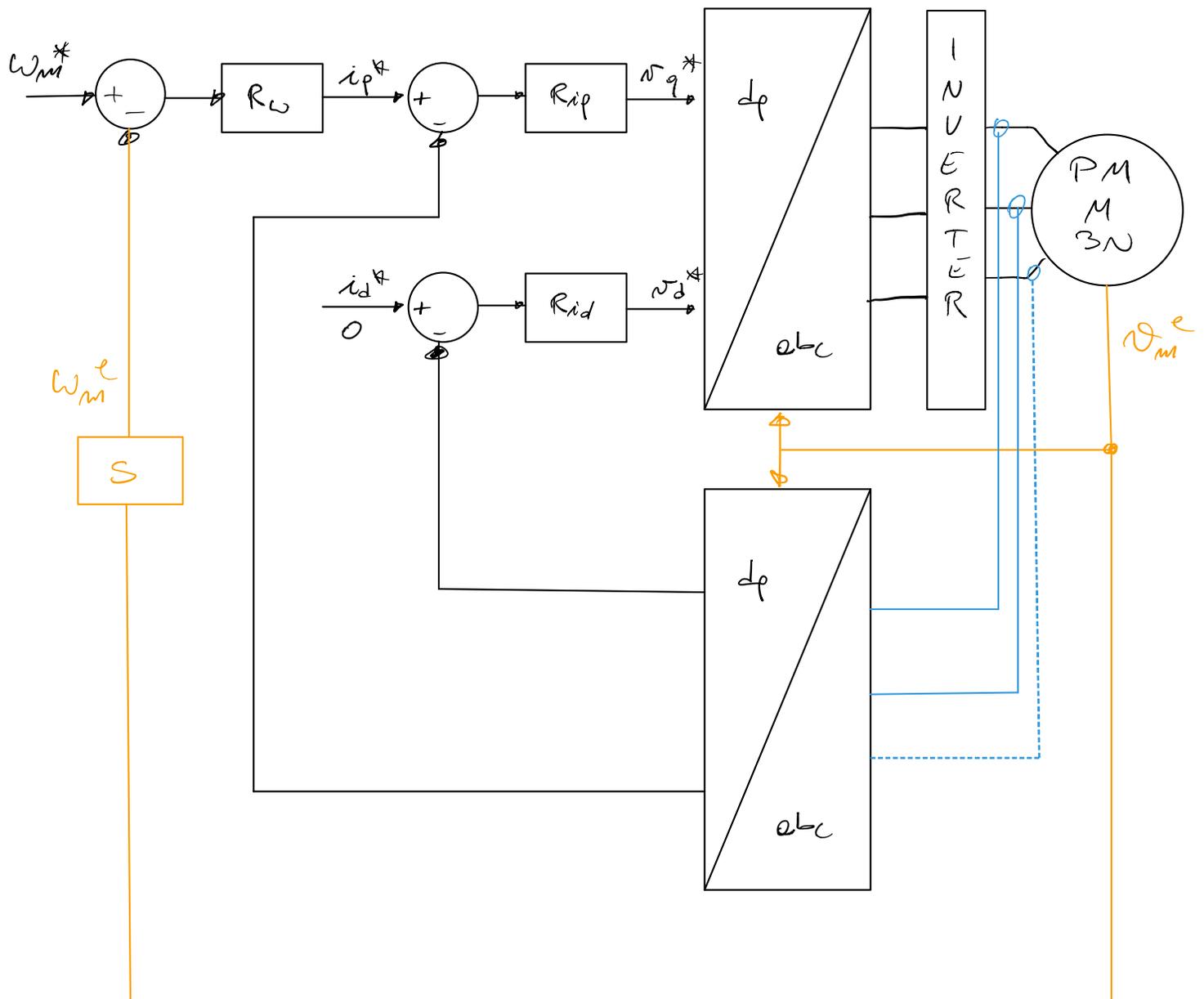
prof. Silverio Bolognani

PARTE III

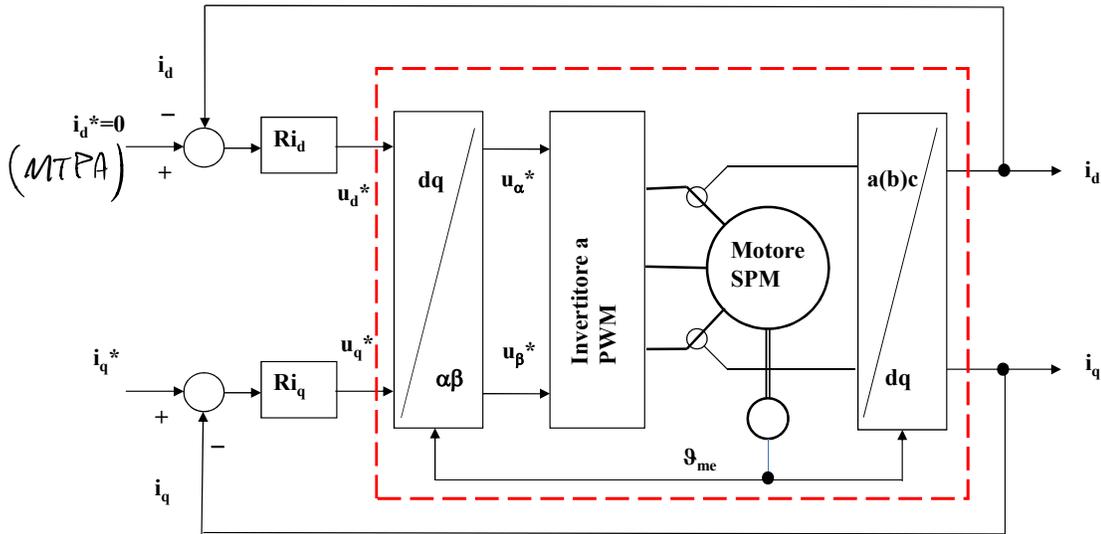
# Controllo di corrente «PID sincro» in azionamenti con motore sincrono



# MACCHINA ISTORICA MTPA



## Schema a blocchi del controllo di corrente dq di un motore SPM

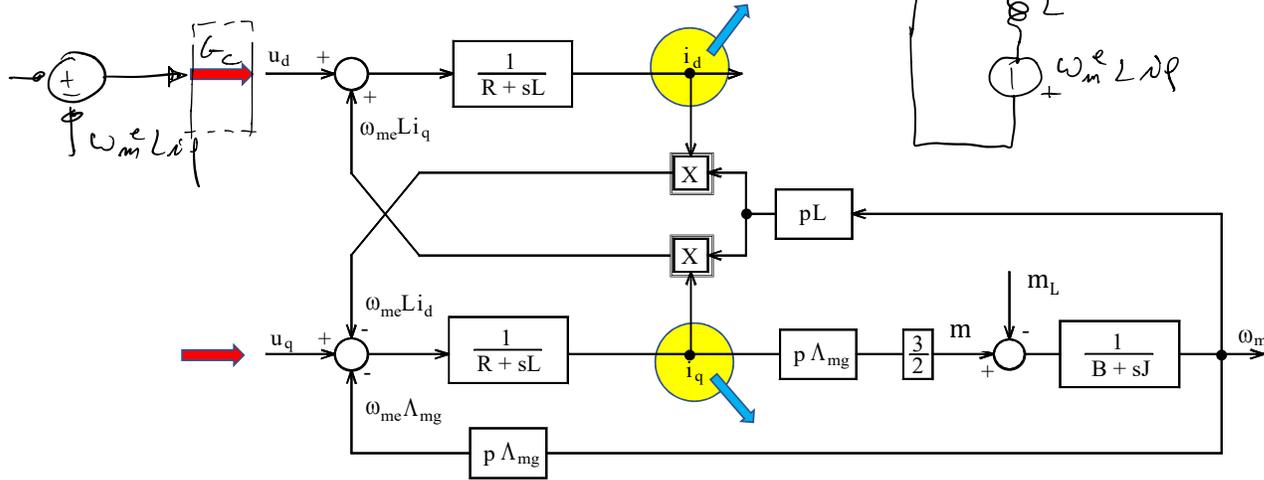


Modello in dq del sistema  
invertitore-motore.

Ingressi: tensioni dqdi  
riferimento (+coppia di  
disturbo)

Uscite: correnti dq

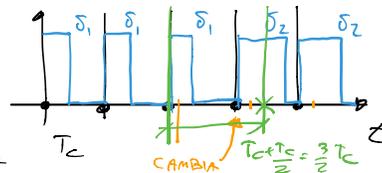
## Dinamica del motore SPM (rotore isotropo)



Nel sistema di riferimento dq la dinamica tensione-corrente del motore SPM è quella di un sistema a **due ingressi** e **due uscite**.

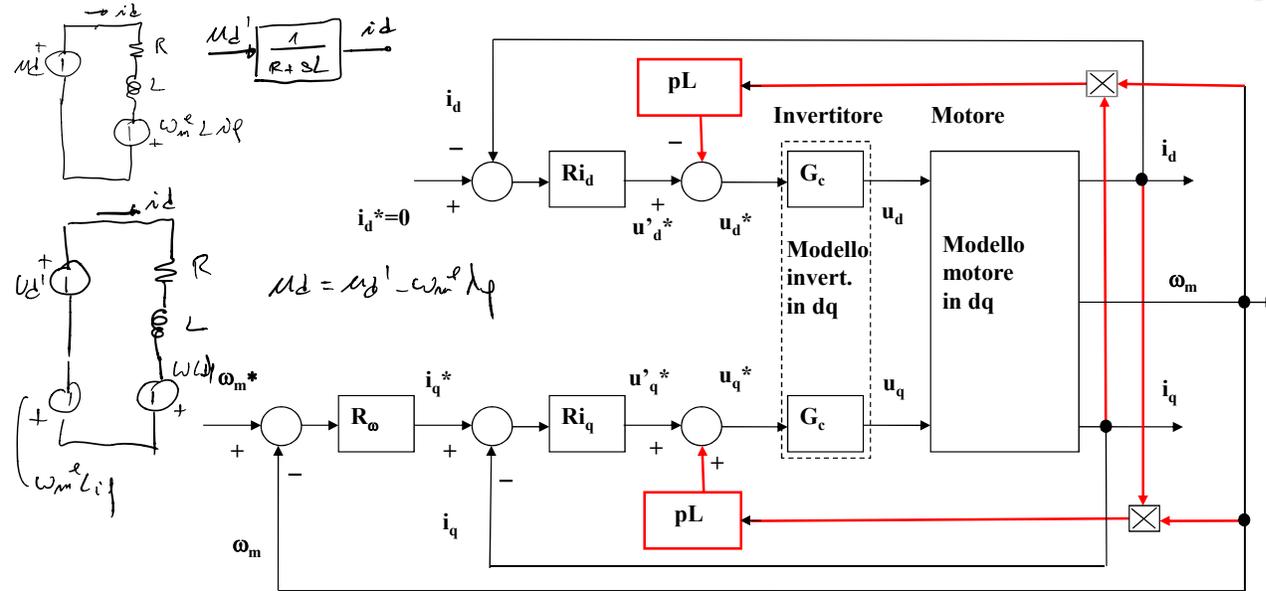
$$G_c = \frac{1}{1 + s T_c}$$

$$T_c = \frac{3}{2} T_c$$



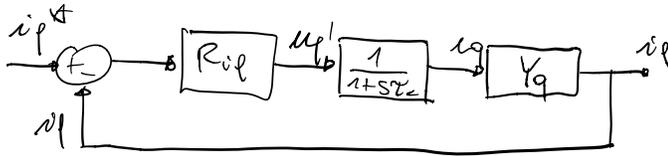
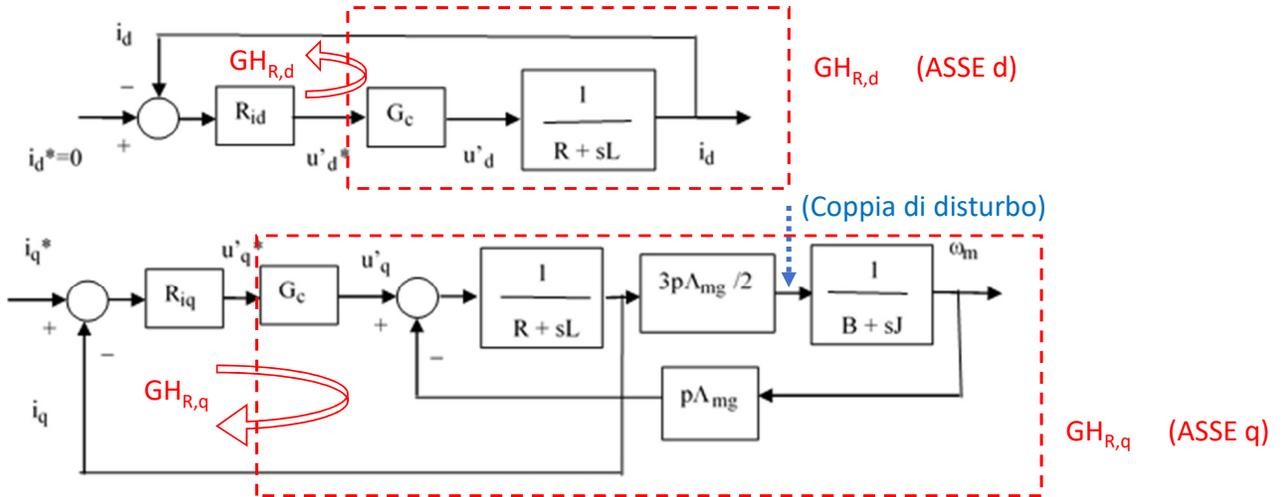
es:  $f_s = 100 \text{ kHz}$   
 $T_c = 10 \mu\text{s}$

## Schema a blocchi del controllo di un azionamento brushless isotropo (SPM)



In rosso le azioni di disaccoppiamento degli assi per trasformare il sistema 2\_IN/2\_OUT in due sistemi 1\_IN/1\_OUT

# Anelli di controllo delle correnti dq dopo disaccoppiamento degli assi



$$GH = \frac{1}{1+s\tau_c} \quad Y_q = \frac{1}{1+s\tau_c} \frac{B+sJ}{\frac{3}{2}(p\Lambda_{mg})^2 \left(1-\frac{s}{p_1}\right) \left(1-\frac{s}{p_2}\right)}$$

$$= \frac{B(1+s\tau_m)}{\frac{3}{2}(p\Lambda_{mg})^2 (1+s\tau_c)(1+s\tau_m)}$$

19-Nov-18

Lezioni di Azionamenti Elettrici a.a. 2018-2019

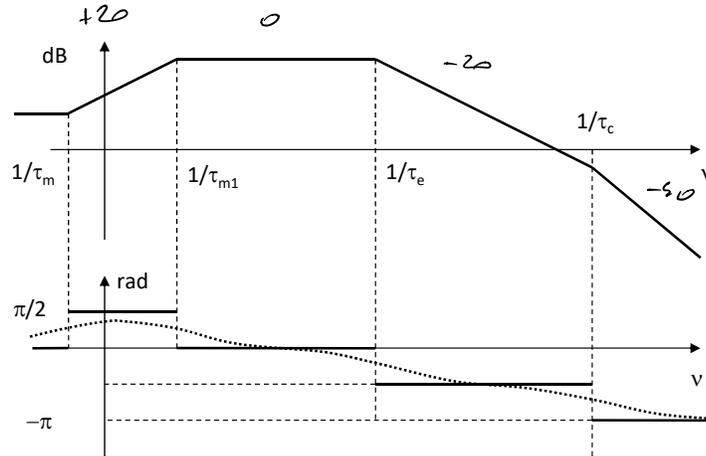
$$\tau_m = \frac{J}{B} \quad \tau_c = \frac{L}{R}$$

$$\tau_{m1} = \frac{JR}{\frac{3}{2}(p\Lambda_{mg})^2}$$

$$\tau_m < \tau_{m1} < \tau_c < \tau_c$$

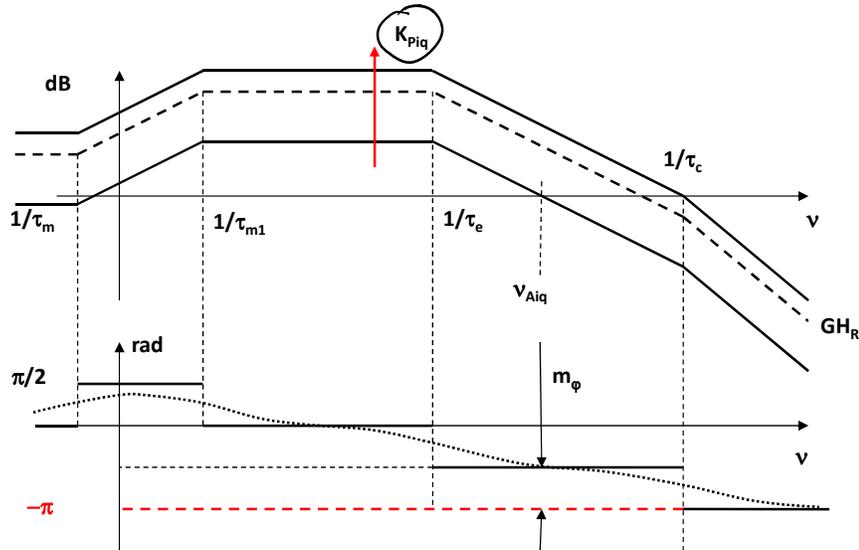
## Diagrammi di Bode di $GH_{R(q)}(j\omega)$

$$GH = \frac{B(1+s\tau_m)}{\frac{s}{2}(p_{lm})^2(1+s\tau_c)(1+s\tau_e)(1+s\tau_{md})}$$



$$R_{iq} = K_{Piq}$$

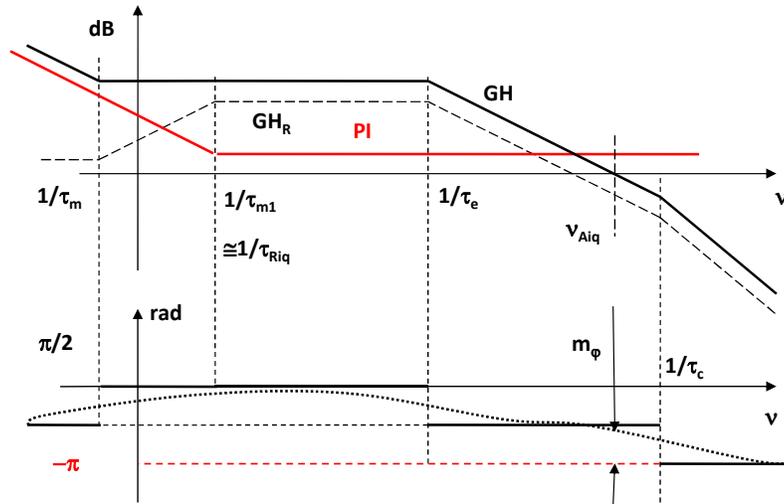
## Diagrammi di Bode di $GH_{(q)}(jv)$ con regolatore $P$



$$R_{ref} = k_P + \frac{k_I}{s} = k_I \frac{1+s\tau_{Rref}}{s} = k_P \frac{1+s\tau_{Rref}}{s\tau_{Rref}}$$

$$\tau_{Rref} = \frac{k_P}{k_I}$$

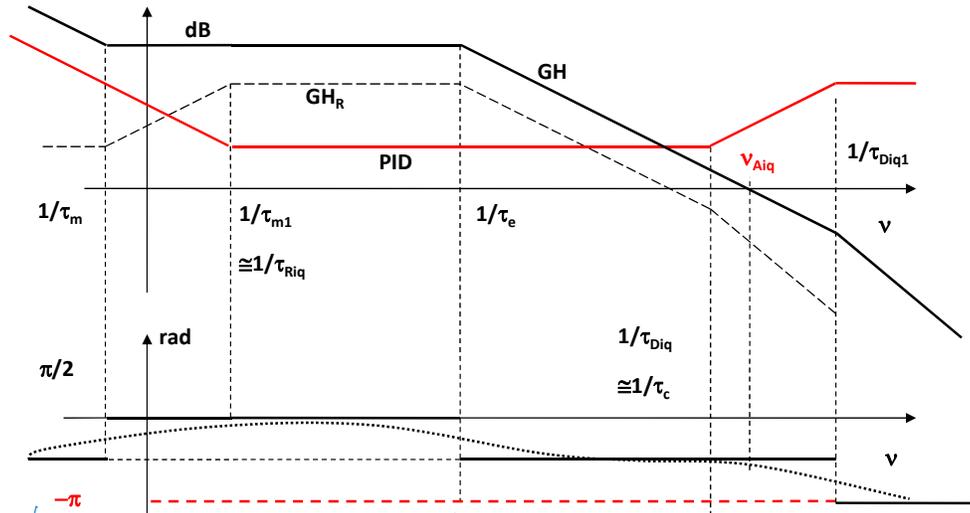
## Diagrammi di Bode di $GH_{(q)}(jv)$ con regolatore PI



ERRORE A REGIME NULO!

$$R_{op} = k_p + \frac{k_i}{s} + s k_D = k_i \frac{(1+s\tau_{Rop})(1+s\tau_{Di1})}{s}$$

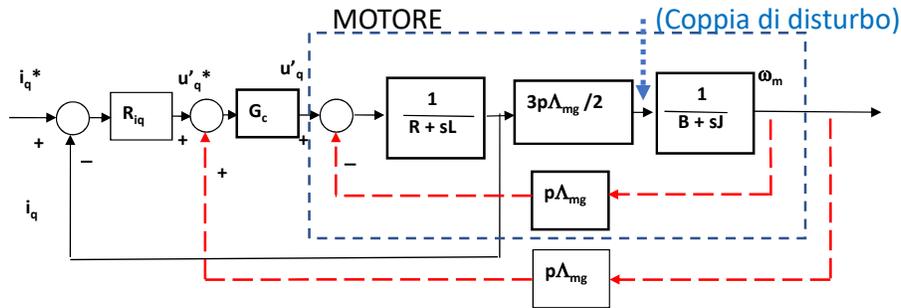
## Diagrammi di Bode di $GH_{(q)}(jv)$ con regolatore PID



$$R_{op} = k_i \underbrace{\frac{1+s\tau_{Rop}}{s}}_{PI} \frac{1+s\tau_{Di1}}{1+s\tau_{Di1}} \quad \text{PI}$$

D: aumento banda passante

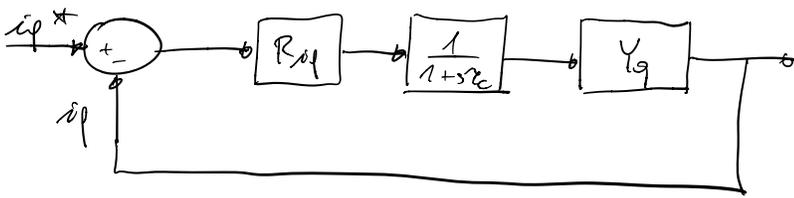
## Schema a blocchi del controllo della corrente in quadratura dopo disaccoppiamento e **compensazione della fem**



In **rosso** l'azione di compensazione della fem

Le fdt dell'anello di asse q non risente dei parametri meccanici e dell'effetto della coppia di disturbo.

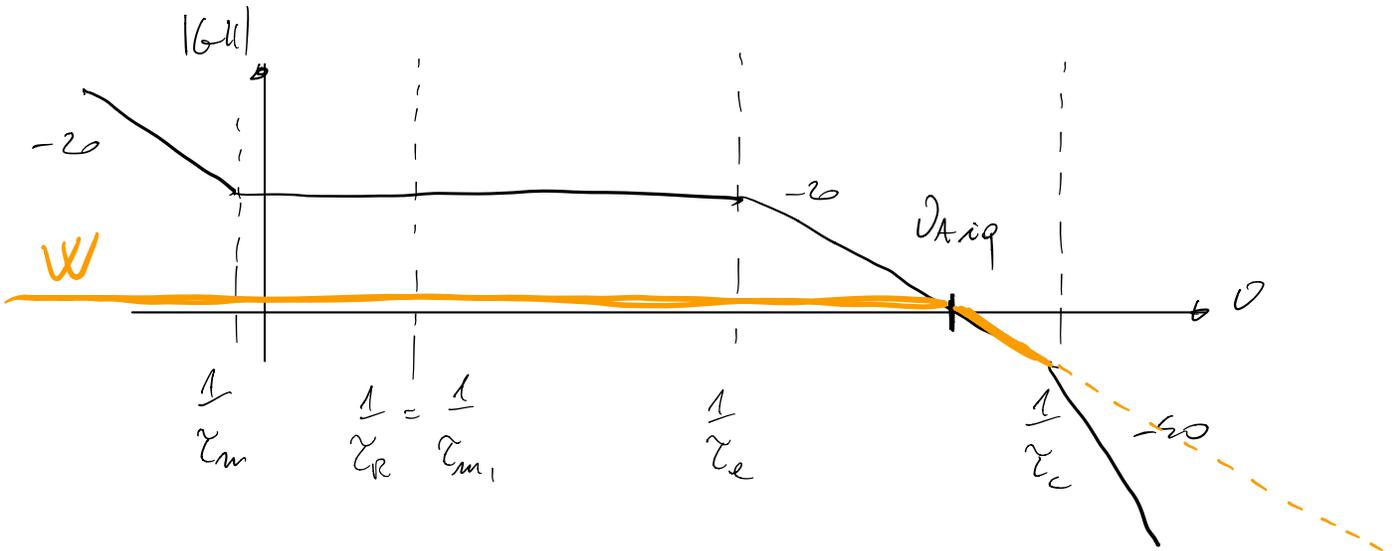
Con motore SPM diventa identica a quella dell'asse d.



$$GH = R_{ol} \frac{1}{1+s\tau_c} Y_g = R_{ol} \frac{1}{1+s\tau_c} \frac{1+s\tau_m}{(1+s\tau_c)(1+s\tau_m)}$$

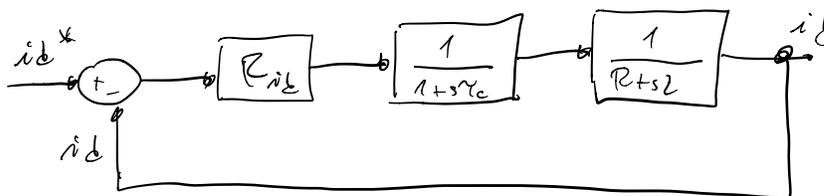
$$= \frac{1+s\tau_R}{s} \frac{1+s\tau_m}{(1+s\tau_c)(1+s\tau_e)(1+s\tau_m)}$$

$$W = \frac{G}{1+GH} = \begin{cases} \approx GH \gg 1 & W = 1 \\ \approx GH \ll 1 & W = G \end{cases}$$



$$W \approx \frac{1}{1+s \frac{1}{\nu_{A,ig}}}$$

Similmente per l'ora 1



ESEMPIO: DIMENSIONARE ANCHE DI CONTROLLO PER UN MOTORE SPM

$$R_s = 1,5 \Omega$$

$$I_m = 0,067 \text{ A}$$

$$L = 5 \text{ mH}$$

$$I_m = 3,1 \text{ A rms}$$

$$M_m = 1,77 \text{ Nm}$$

$$P = 4$$

$$J = 0,28 \cdot 10^{-3} \text{ kg m}^2$$

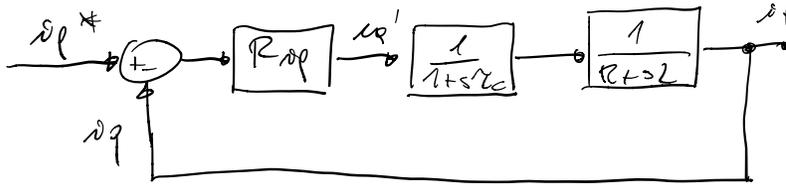
$$B = 0,00192 \frac{\text{Nm}}{\text{rad/s}}$$

$$U_m = 85 \text{ V (rms)}$$

$$\omega_{mm} = 512 \frac{\text{rad}}{\text{s}} \quad P_m = 750 \text{ W}$$

$$T = 100 \mu\text{s}$$

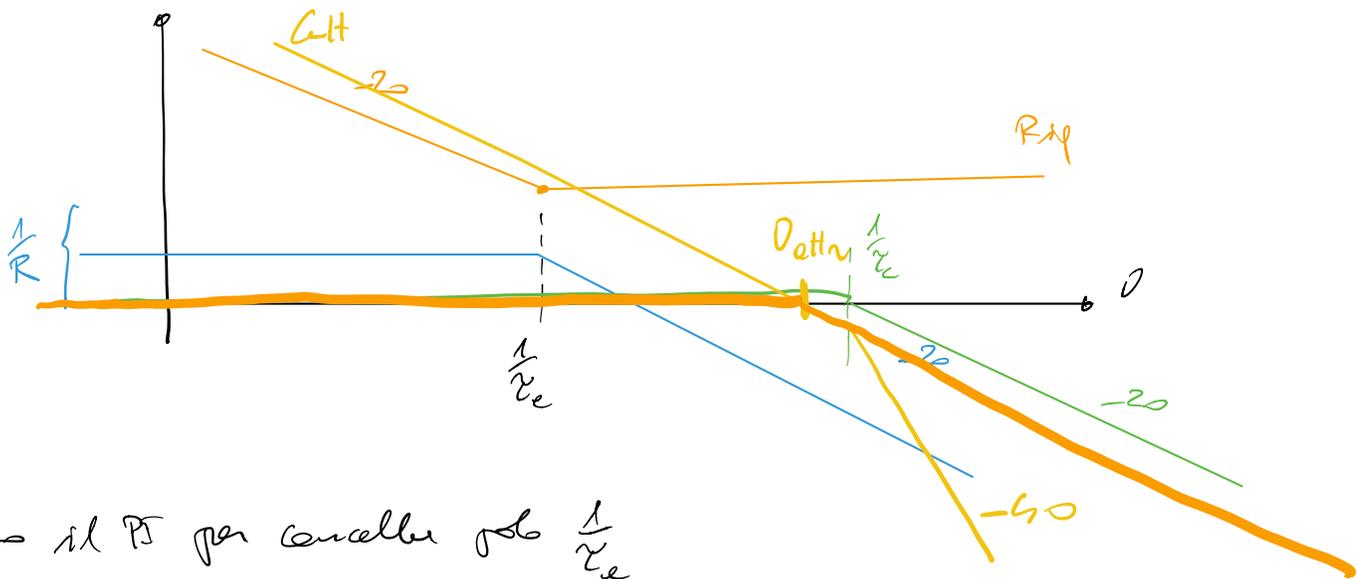
USO DI STRATEGIA PIU' ASSI E COMPUNTA DI UN F. CEM.



$$\frac{1}{R+sL} = \frac{1/R}{1+s \frac{L}{R}} = \frac{1/R}{1+s T_c}$$

$$T_c = \frac{L}{R} = \frac{5 \cdot 10^{-3}}{1,5} = 3,3 \text{ ms}$$

$$T_c = \frac{3}{2} T = 1,5 \cdot 100 \mu = 150 \mu\text{s}$$



USO IL PIU' PER CONSERVARE IL  $\frac{1}{T_c}$

$$K_R = K_p \frac{1+s T_{Rq}}{s T_{Rq}}$$

$$\frac{1}{T_{Rq}} = \frac{1}{T_c} = \frac{1}{3,3 \cdot 10^{-3}} = 285,7$$

Scelgo  $M_p = 70^\circ = 180 + \arg G(s) D_{etn}$

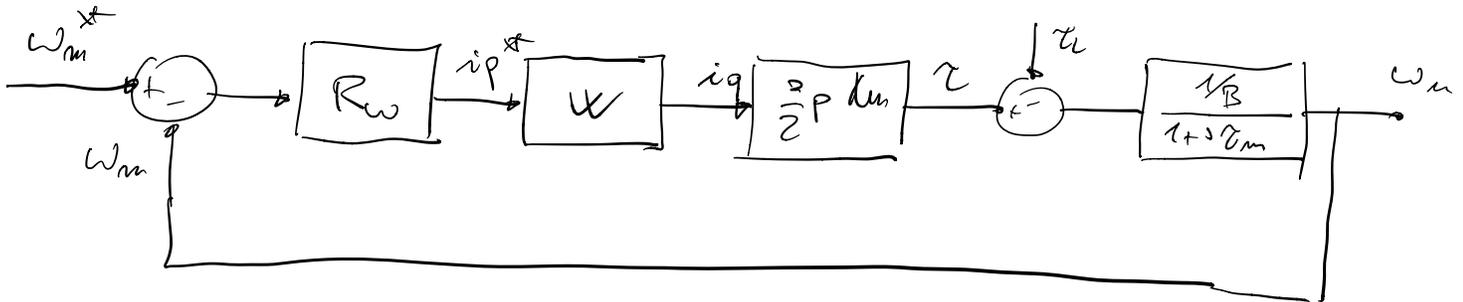
$$D_{etn} = \frac{\tan 20^\circ}{150 \cdot 10^{-6}} = 2926 \frac{\text{rad}}{\text{s}}$$

$$W = \frac{1}{1+s \frac{1}{D_{etn}}} = \boxed{\frac{1}{1+s \cdot 4,12 \cdot 10^{-5}}}$$

Calcolo  $K_p$

$$|G_{tot}(0_{detn})| = 1 \dots K_p = 14,87 \frac{V}{A}$$

$$R_{iq} = K_p \frac{1+s\tau_{cm}}{s\tau_{cm}} = \boxed{14,87 \frac{1+s \cdot 3,5 \cdot 10^{-3}}{s \cdot 3,5 \cdot 10^{-3}}}$$



$$R_w = K_{pw} \frac{1+s\tau_{iw}}{s\tau_{iw}}$$

$$\tau_{iw} = \tau_m = \frac{J}{B} = \frac{0,29 \cdot 10^{-3}}{900 \text{ kg/m}^2} = 9,15 \text{ s}$$

Impiego  $M\phi = 70^\circ = 180 + \arg G_{tot}(0_{detn}^w)$

$$\omega_{detn} = 631,5 \frac{\text{rad}}{\text{s}} \quad \left( \omega_{detn} = 2626 \frac{\text{rad}}{\text{s}} \text{ ANGICO DI GERONTO} \right)$$

Impiego  $|G_{tot}(0_{detn}^w)| = 1 \Rightarrow K_{pw} = 0,58$

$$R_w = 0,58 \frac{1+0,15s}{s \cdot 9,15}$$

SIMULAZIONE IN SIMULINK!