

ESEMPIO 1 : Dato il seguente motore

$$2p = 4$$

$$R = 2 \Omega$$

$$L_d = 40 \text{ mH}$$

$$L_q = 40 \text{ mH}$$

$$\xi = \frac{L_q}{L_d} = 4$$

$$\omega_m = 150 \frac{\text{rad}}{\text{s}}$$

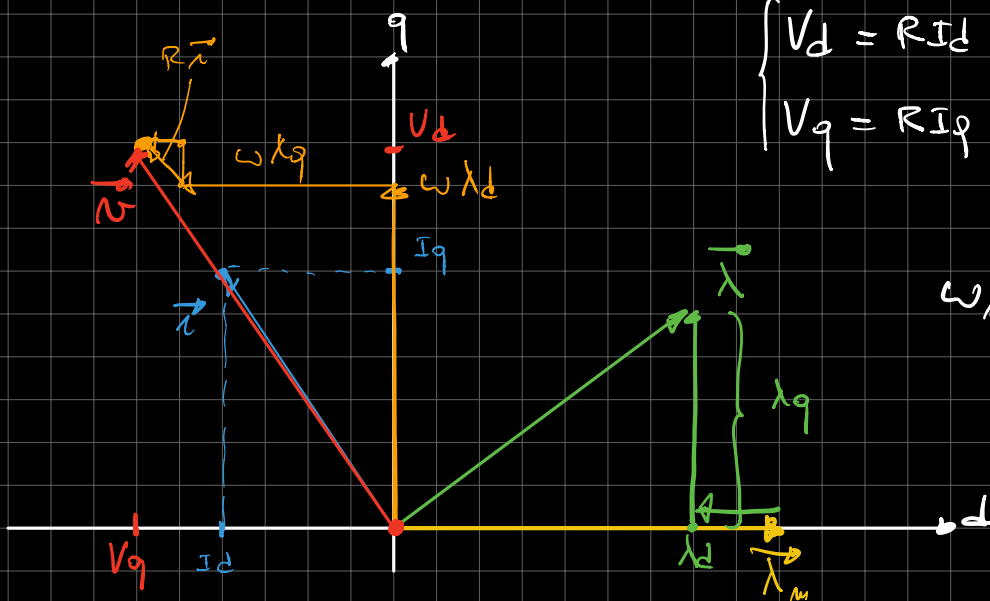
$$I_d = -8,5 \text{ A}$$

$$I_q = 12 \text{ A}$$

} Picco

$$\lambda_m = 0,6 \text{ Vs (picco)}$$

? Calcolare tensione necessaria, bilancio delle potenze



$$\begin{cases} V_d = R I_d - \omega_m^e L_q I_q \\ V_q = R I_q + \omega_m^e (\lambda_m + L_d I_d) \end{cases}$$

$\lambda_q = 0,58$   
 $\lambda_d = 0,515 \text{ Vs}$

$$\omega_m^e = \omega_m \cdot p = 150 \cdot 2 = 300 \frac{\text{rad}}{\text{s}}$$

$$\lambda_d = \lambda_m + L_d I_d = 0,6 - 0,04 \cdot 8,5 = 0,515 \text{ Vs}$$

$$\lambda_q = L_q I_q = 0,04 \cdot 12 = 0,48 \text{ Vs}$$

$$\begin{cases} V_d = \dots = 2(-8,5) - 300 \cdot 0,48 = -161 \text{ V} \\ V_q = \dots = 2 \cdot 12 + 300 \cdot 0,515 = 178,5 \text{ V} \end{cases}$$

$$\vec{V} = 240,4 \text{ e}^{j132^\circ}$$

$$\text{Coppie : } m = \frac{3}{2} p [\lambda_m I_q + (L_d - L_q) I_d I_q]$$

$$= \frac{3}{2} \cdot 2 [0,6 \cdot 12 + (40 - 40) \cdot 10^{-3} (-8,5) \cdot 12]$$

$$= 30,8 \text{ Nm}$$

$$P_m = m \cdot \omega_m = 30,8 \cdot 150 = 4617 \text{ W}$$

$$P_J = \frac{3}{2} R I^2 = \frac{3}{2} \cdot 2 \cdot (I_d^2 + I_q^2) = 698,8 \text{ W}$$

$$P_{in} = P_m + P_J = 5617 + 698,8 = 5265 \text{ W}$$

$$= \frac{3}{2} (V_d I_d + V_q I_q) = \frac{3}{2} ((-161)(-8,5) + 178,5 \cdot 12) = 5265 \text{ W}$$

$$\eta = \frac{P_m}{P_{in}} = \frac{5617}{5265} = 0,877 \quad 87,7\%$$

## ESEMPIO 2 motore a Reluttanze

Dati il seguente motore:

$2p = 6$   
 $\lambda_m = 0$  (R&C)  
 $R \approx 0$  trascurabile

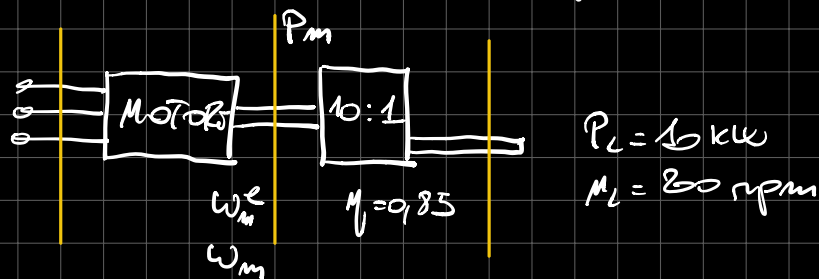
$L_d = 50 \text{ mH}$   
 $L_q = 10 \text{ mH}$

Si è collegato ad un carico meccanico con le seguenti caratteristiche

$P_L = 10 \text{ kW}$  e si è collegato al motore mediante riduttore di giri con rapporto  $1:10$   $\eta = 0,85$

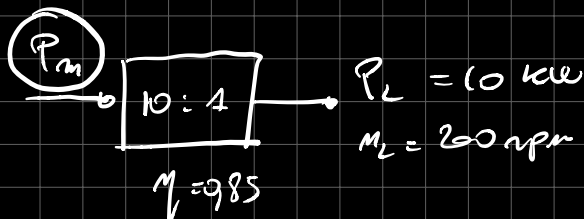
$M_L = 200 \text{ rpm}$

$i_d = V$   
 $i_q = V$   
 $f = V$



$$m = \frac{3}{2} p \left[ \lambda_m I_q + (L_d - L_q) I_d I_q \right] = \frac{3}{2} p (L_d - L_q) I_d I_q \quad L_d > L_q$$

$I_d, I_q > 0 \quad I^\circ \text{ frecciate}$



$$P_m = \frac{P_L}{\eta} = \frac{10 \cdot 10^3}{0,85} = 11675 \text{ W}$$

$$M_m = 2000 \text{ rpm}$$

$$\omega_m = \frac{2000 \text{ rpm}}{60} = 209,3 \frac{\text{rad}}{\text{s}}$$

$$\omega_m^e = p \cdot \omega_m = 3 \cdot 209,3 = 628 \frac{\text{rad}}{\text{s}}$$

$$f = \frac{\omega_m}{2\pi} = \frac{628}{2\pi} = 100 \text{ Hz} \quad \text{frequenze di alimentazione del motore}$$

$$P_m = m \cdot \omega_m \quad m = \frac{P_m}{\omega_m} = \frac{11675}{209,3} = 55,78 \text{ Nm}$$

$$m = \frac{3}{2} p(L_d - L_q) I_d I_q = 55,78 \text{ Nm}$$

$$= \frac{3}{2} p(L_d - L_q) I \cos \alpha_i I \sin \alpha_i$$

$$= \frac{3}{2} p(L_d - L_q) \frac{I^2}{2} \sin 2\alpha_i$$

$$\sin 2\alpha_i = 1 \quad \text{ha } |I| \text{ minime MTPA}$$

$$\alpha_i = 45^\circ \quad I_d = I_q = \frac{I}{\sqrt{2}}$$

$$m = \frac{3}{2} p(L_d - L_q) \frac{I^2}{2} = 55,78 \text{ Nm}$$

$$I = \sqrt{\frac{4m}{3p(L_d - L_q)}} = \sqrt{\frac{4 \cdot 55,78}{3 \cdot 3(50 - 10) \cdot 10^{-3}}} = 29,9 \text{ A}$$

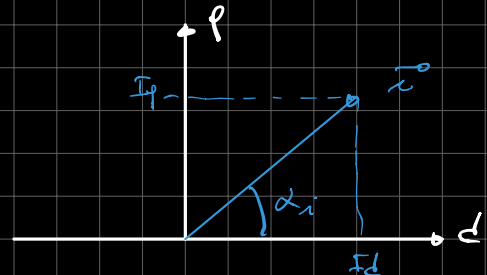
$$\vec{i} = 29,9 e^{j45^\circ}$$

$$I_d = I_q = \frac{29,9}{\sqrt{2}} = 17,6$$

$$V_d = R I_d - \omega_m^2 L_q I_q = -\omega_m^2 L_q I_q = -628 \cdot 10 \cdot 10^{-3} \cdot 17,6 = -110,5 \text{ V}$$

$$V_q = R I_q + \omega_m^2 L_d I_d = \omega_m^2 L_d I_d = 628 \cdot 50 \cdot 10^{-3} \cdot 17,6 = 550 \text{ V}$$

$$\vec{V} = 564 e^{j101,5^\circ}$$



$$\vec{i} = I_d + j I_q = I e^{j\alpha_i}$$

$$I^2 = I_d^2 + I_q^2$$

$$I_d = I \cos \alpha_i$$

$$I_q = I \sin \alpha_i$$

# Regioni limite di funzionamento

$$I_m \quad U_m \quad \rightarrow \quad I_d \quad I_q$$

$$|\vec{i}| \leq I_m \quad |\vec{v}| \leq U_m$$

$$I_q^2 + I_d^2 \leq I_m^2$$

CERCHIO DI RAGGIO  
 $I_m$

$$\begin{cases} U_d = R I_d - \omega_m^2 L_q I_q \\ U_q = R I_q + \omega_m^2 (\lambda_m + L_d I_d) \end{cases}$$

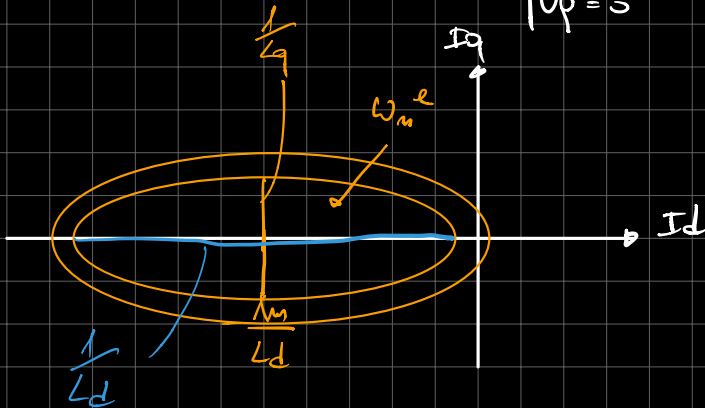
$$U_d^2 + U_q^2 \leq U_m^2$$

$$\omega_m^2 (L_q I_q)^2 + \omega_m^2 (\lambda_m + L_d I_d)^2 \leq U_m^2$$

$$(\lambda_m + L_d I_d)^2 + (L_q I_q)^2 \leq \left(\frac{U_m}{\omega_m}\right)^2$$

$L_d \neq L_q$  ECCENTRO DI TENSIONE

CENTRO  $\begin{cases} U_d = 0 \\ U_q = 0 \end{cases} \quad \begin{cases} I_q = 0 \\ I_d = -\frac{\lambda_m}{L_d} = I_{ch} \end{cases}$

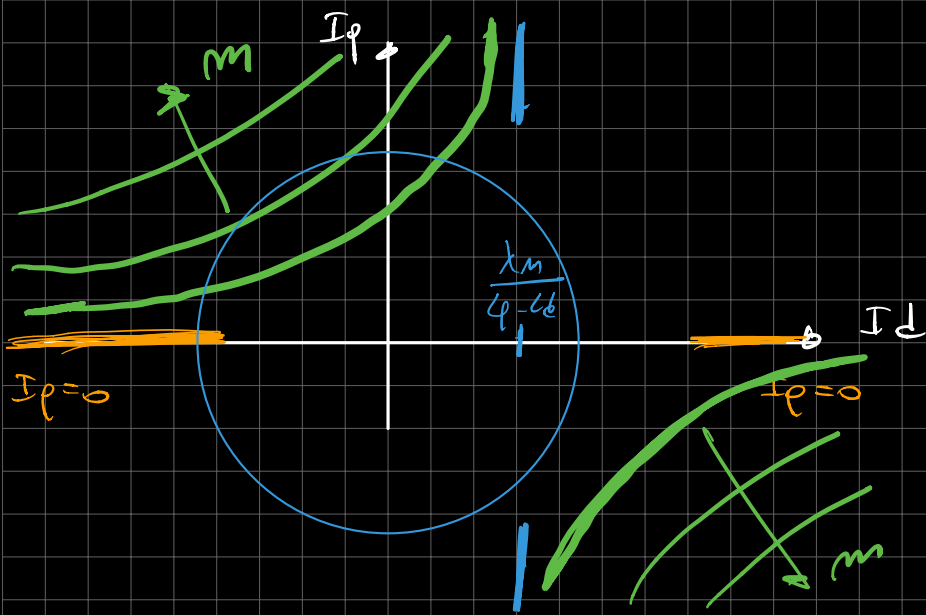


$$SACIENZA = \frac{\frac{1}{L_d}}{\frac{1}{L_q}} = \frac{L_q}{L_d} \rightarrow$$

$$m = \frac{3}{2} p [\lambda_m I_q + (L_d - L_q) I_d I_q] = \frac{3}{2} p I_q [\lambda_m + (L_d - L_q) I_d]$$

$$I_q = \frac{2}{3} \frac{m}{p [\lambda_m + (L_d - L_q) I_d]}$$

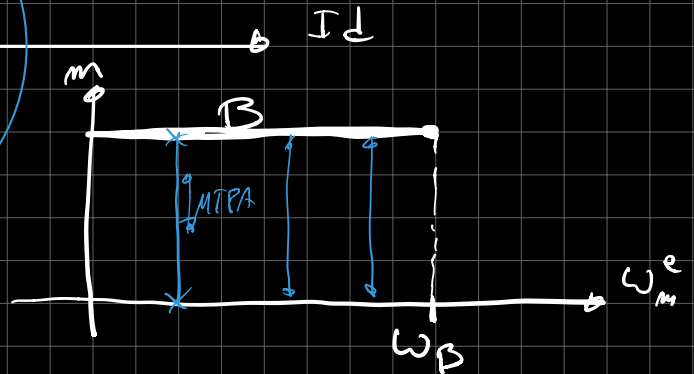
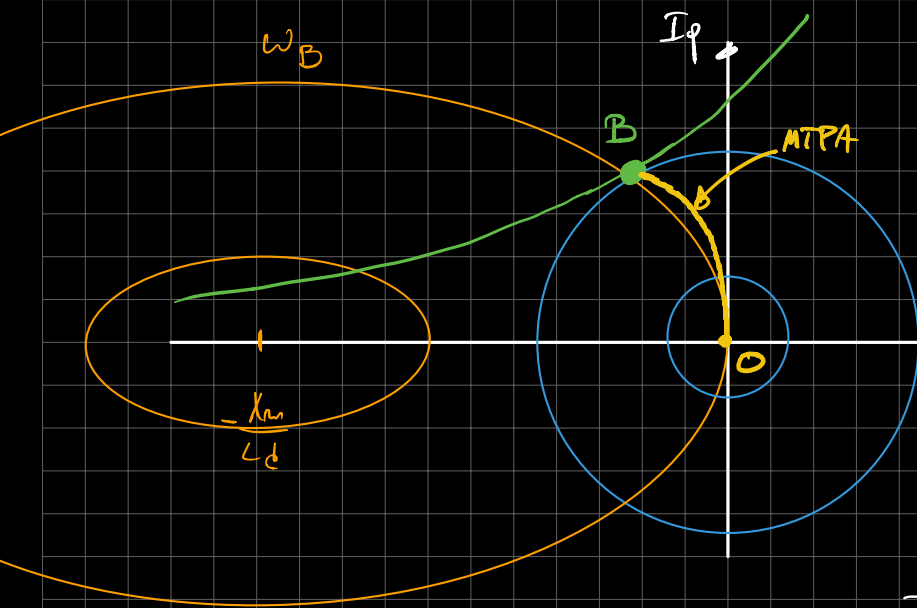
iperbole con  
asintoti  $\begin{cases} I_q = 0 \\ I_d = \frac{\lambda_m}{L_q - L_d} \end{cases}$



TUTTO IL PUNTO DI CONTATTO

B: punto base

OB MTPA



① Impongo la tangente fra isocrono e cerchio di corrente

$$I_d = I \cos \alpha$$

$$I_q = I \sin \alpha$$

$$m = \frac{3}{2} p \left[ \lambda_m I \sin \alpha + \underbrace{(L_d - L_q) I^2 \sin^2 \alpha}_{\frac{8m^2 \alpha_i}{2}} \right]$$

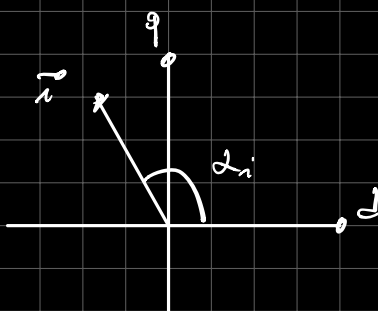
$$\frac{dm}{d\alpha_i} = 0 = \lambda_m I \cos \alpha_i + (L_d - L_q) I^2 \cos 2\alpha_i$$

$$= \lambda_m \cos \alpha_i + (L_d - L_q) I \cos 2\alpha_i$$

$$= \lambda_m \cos \alpha_i + (L_d - L_q) I (2 \cos^2 \alpha_i - 1)$$

$$\underbrace{2(L_d - L_q) I}_{a} \underbrace{\cos^2 \alpha_i}_{m} + \underbrace{\lambda_m}_{b} \underbrace{\cos \alpha_i}_{m} - \underbrace{(L_d - L_q) I}_{c} = 0$$

$$\cos \alpha_i = \frac{-\lambda_m \pm \sqrt{\lambda_m^2 + 8(L_d - L_q)^2 I^2}}{4(L_d - L_q) I}$$



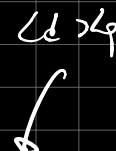
$$4(L_d - L_q) I$$

$L_d < L_q \rightarrow < 0$

$$\cos \alpha_i < 0$$

$$\alpha_i > \frac{\pi}{2}$$

Nota se  $\lambda_m = 0$   $\cos \alpha_i = \frac{-\sqrt{8}}{4} = -\frac{\sqrt{2}}{2}$   $135^\circ = 90^\circ + 45^\circ$



$$I_d = I \cos \alpha_i = \frac{-\lambda_m + \sqrt{\lambda_m^2 + 8(L_d - L_q)^2 I^2}}{4(L_d - L_q)}$$

$$I_q = \sqrt{I^2 - I_d^2}$$

$$\textcircled{2} \quad m = \frac{3}{2} P \left[ \lambda_m I_q + (L_d - L_q) I_d I_q \right]$$

$$I_q = f(I_d)$$

$$I_q = \frac{2}{3} \frac{m}{P} \frac{1}{\lambda_m + (L_d - L_q) I_d}$$

CALCOLO  $\omega_B$

$$\begin{cases} U_d = -\omega_B \lambda_p = -\omega_B C_p I_q \\ U_q = \omega_B (\lambda_m + L_d I_d) \end{cases}$$

$$U_d^2 + U_q^2 = V_m^2$$

$$\omega_B = \dots$$